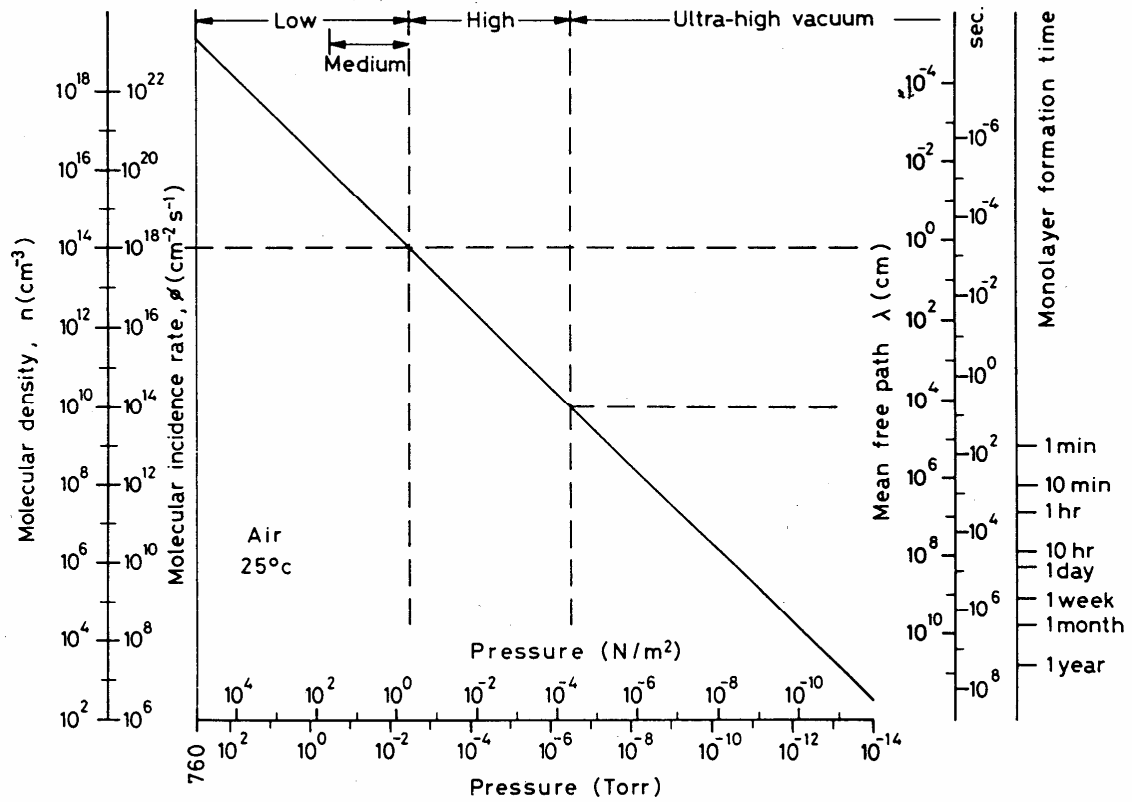


Appendix

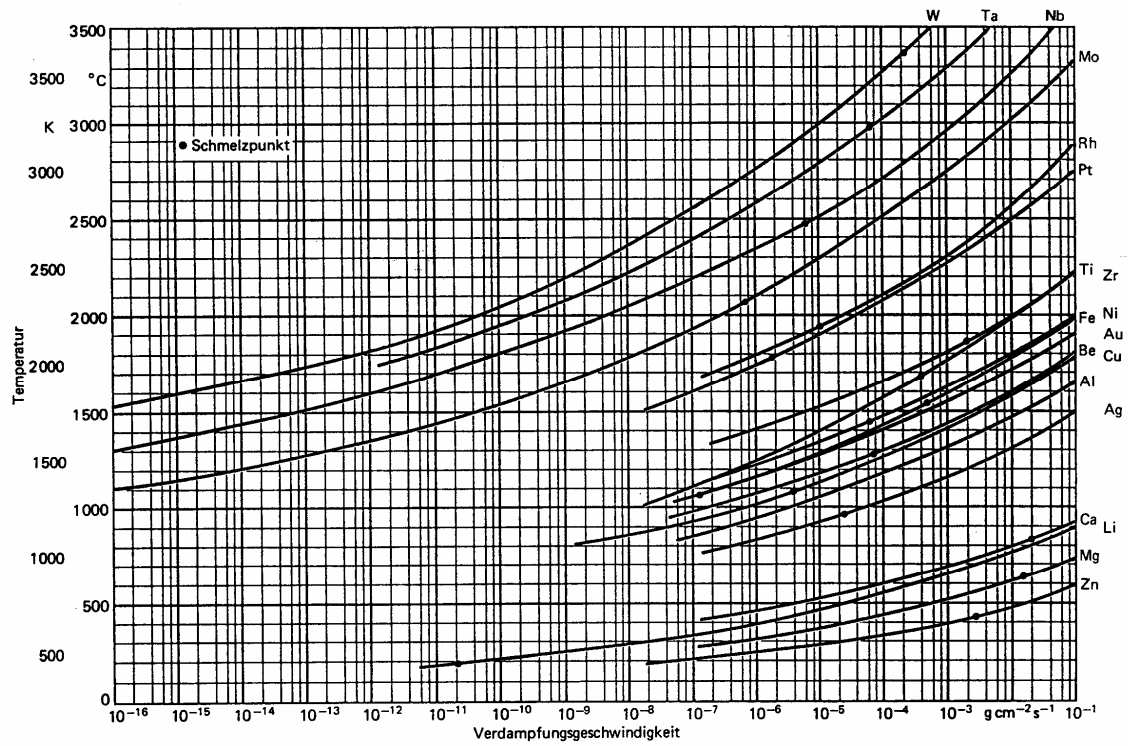
Vacuum Technique:



Time for the formation of a monolayer in dependence on the ambient pressure
 Particle density n , impingement rate Φ , mean free path λ
 [13, p. 2]

Appendix

Evaporation Technique:



Evaporation velocity in high vacuum in dependence on the source temperature
[3, p. 20]

Appendix

Sputtering:

Target	Sputterausbeute Y für E_i in eV						E_{thres}	E_0
	200	600	1 000	2 000	5 000	10 000		
	Atome/Ion							
Ag	1,6	3,4				8,8	15	2,94
Al	0,35	1,2			2,0		13	3,33
Au	1,1	2,8	3,6	5,6	7,9		20	3,92
C	0,05	0,2					-	7,39
Co	0,6	1,4					25	4,40
Cr	0,7	1,3					22	4,11
Cu	1,1	2,3	3,2	4,3	5,5	6,6	17	3,50
Fe	0,5	1,3	1,4	2,0	2,5		20	4,13
Ge	0,5	1,2	1,5	2,0	3,0	3,98	25	-
Mo	0,4	0,9	1,1		1,5	2,2	24	6,88
Nb	0,25	0,65					25	-
Ni	0,7	1,5	2,1				21	4,45
Os	0,4	0,95					-	8,19
Pd	1,0	2,4					20	3,90
Pt	0,6	1,6					25	5,95
Re	0,4	0,9					35	8,06
Rh	0,55	1,5					24	5,76
Si	0,2	0,5	0,6	0,9	1,4		-	4,68
Ta	0,3	0,6			1,05		26	8,10
Th	0,3	0,7					24	5,97
Ti	0,2	0,6		1,1	1,7	2,1	20	4,86
U	0,35	1,0					23	5,00
W	0,3	0,6			1,1		33	8,80
Zr	0,3	0,75					22	6,34
Moleküle/Ion								
CdS (1010)	0,5	1,2						
GaAs (110)	0,4	0,9						
GaP (111)	0,4	1,0						
GaSb (111)	0,4	0,9	1,2					
InSb (110)	0,25	0,55						
PbTe (110)	0,6	1,40						
SiC (0001)		0,45						
SiO ₂			0,13	0,4				
Al ₂ O ₃			0,04	0,11				

Sputter yield Y of different materials as a function of the energy E_i of impinging Ar-Ions, threshold energy E_{thres} and sublimation energy E_0 [1, p. 98]

Appendix

Analytical Methods:

Tabelle 8-7. Analysemethoden und ihre Charakterisierungsart.

Methode	Abkürzungen	Anregung/ Detek- tion*)	Charakterisierungsart			elek- tronische Eigen- schaften	Referenzen
			Chemische Analyse	Molekül- kristall- strukturen	Mikro- skopie		
Light Microscopy	LM	$h\nu \rightarrow h\nu$			x		[8-335]
Laser Scanning Microscopy	LSM	$h\nu \rightarrow h\nu$			x		[8-314; 8-416]
Ramanscattering	RS	$h\nu \rightarrow h\nu$		x			[8-395; 8-398 bis 8-402]
X-ray Photoelectron Spectrosc.	XPS	$h\nu \rightarrow c$	x				[8-340; 8-341; 8-434 bis 8-437]
Ultra Violet PS	UPS	$h\nu \rightarrow c$				x	[8-435; 8-436]
Laser Microprobe Mass Anal.	LAMMA	$h\nu \rightarrow i$	x				[8-438]
Photo Acoustic Spectroscopy	PAS	$h\nu \rightarrow ph$			x		[8-403]
Scanning Electron Microscopy	SEM	$e \rightarrow e$			x		[8-467; 8-430; 8-431; 8-432]
(Scan)Transmission Electr. Micr.	(S)TEM	$e \rightarrow e$		x			[8-466; 8-463 bis 8-466]
Electron Beam Induced Current	EBIC	$e \rightarrow e$			x	x	[8-467; 8-468; 8-469]
Voltage Contrast Microscopy	VCM	$e \rightarrow c$			x	x	[8-335]
Low Energy Electron Diffraction	LEED	$e \rightarrow c$		x			[8-357; 8-408; 8-409]
Reflective High EED	RHEED	$e \rightarrow c$		x			[8-359; 8-418; 8-419]
Auger Electron Spectroscopy	AES	$e \rightarrow e$	x		x		[8-340; 8-433; 8-434]
Electron Energy Loss Spectr.	EELS	$e \rightarrow e$	x	x		x	[8-357; 8-404 bis 8-407]
Electron Micro Probe	EMP	$e \rightarrow h\nu$	x				[8-439]
X-Ray Emission Spectroscopy	XES	$c \rightarrow h\nu$	x		x		[8-431; 8-432; 8-458; 8-459; 8-460]
Ion Scattering Spectroscopy	ISS	$i \rightarrow i$	x	(x)			[8-340; 8-410; 8-434]
Secondary Ion Mass Spectrosc.	SIMS	$i \rightarrow i$	x		x		[8-340; 8-346; 8-354; 8-440; 8-441; 8-442]
Rutherford Backscattering	RBS	$i \rightarrow i$	x	(x)			[8-454; 8-455; 8-456]
Secondary Neutral Mass Spectr.	SNMS	$i \rightarrow n$	x				[8-355]
Particle Induced X-Ray Emission	PIXE	$i \rightarrow h\nu$	x				[8-356]
Field Ion Microscopy	FIM	$e \rightarrow i$	x	x			[8-340]
Scanning Tunneling Microscopy	STM	$e \rightarrow e$		x	x	(x)	[8-428; 8-429]
Scanning Acoustic Microscopy	SAM	$ph \rightarrow ph$			x		[8-416; 8-417]

*) $h\nu$ Photonen, ph Phononen, e Elektronen, i Ionen, n Neutralteilchen, e elektrisches Feld

[3, p. 342]

Appendix

Calculation of the conductivity of thin films:

The starting point of all following considerations is the current density \vec{j}_e ,

$$\vec{j}_e = -ne\vec{v} = -e\vec{v} \int_N \frac{dn}{V} = -e\vec{v} \frac{N}{V} = -ne\vec{v}$$

Since e and \vec{v} are known, the electron density n has to be calculated:

$$dn = 2 \cdot f_0(E) \cdot d\Phi \quad d\Phi \dots \text{Phase space volume}$$

$$f_0(E) = \frac{1}{1 + e^{(E-E_f/k_B T)}} \dots \text{Fermi-distribution}$$

$$d\Phi = \frac{d^3x d^3p}{h^3} \dots \text{dimensionless, number of states in a phase space element of the size } d^3x d^3p$$

From quantum mechanics the number of possible states within a phase space element with the generalized coordinates (q,p) : $\frac{d^3q d^3p}{h^3}$ is known: in a phase space element of the size h^3 there can be only one state

a) Conductivity without electric field

$$\begin{aligned} \vec{j}_e &= -e \int_{R,\vec{v}} \vec{v} \frac{dn}{V} = -2e \int_{R,\vec{v}} \vec{v} f_0(\vec{v}) \frac{d\Phi}{V} = \left| d\Phi = \left(\frac{m}{h} \right)^3 d^3x d^3v \right| = \\ &= -2e \left(\frac{m}{h} \right)^3 \frac{1}{V} \cdot \underbrace{\int_R d^3x}_{\vec{v}} \int_{\vec{v}} \vec{v} f_0(\vec{v}) d^3v = -2e \left(\frac{m}{h} \right)^3 \int_{\vec{v}} \vec{v} f_0(\vec{v}) d^3v = 0 \end{aligned}$$

b) Conductivity with electric field in an infinite medium: Ohm's law

Application of Boltzmann's transport theory:

General formulation of Boltzmann's equation:

$$\frac{df(\vec{r}, \vec{v}, t)}{dt} = \left(\frac{\mathcal{D}f}{\mathcal{D}\vec{r}} \right)_{coll}$$

i. e. changes in the distribution function are only due to collisions (extremely short interactions of the components of the system).

Total differential:

$$\frac{\mathcal{F}}{\partial t} + \vec{\nabla}_r f \frac{d\vec{r}}{dt} + \vec{\nabla}_v f \frac{d\vec{v}}{dt} = \left(\frac{\mathcal{F}}{\partial t} \right)_{coll}$$

$a = \vec{F}/m = -\frac{e\vec{E}}{m}$

Special shape of Boltzmann's equation for the electric field:

$$\frac{\mathcal{F}}{\partial t} + \vec{v} \vec{\nabla}_r f - \frac{e\vec{E}}{m} \vec{\nabla}_v f = \left(\frac{\mathcal{F}}{\partial t} \right)_{coll}$$

Ansatz for the collision term determines the detailed solution of Boltzmann's equation:

$$f(t) - f_0 = C \cdot e^{-t/\tau}$$

$$\left(\frac{\mathcal{F}}{\partial t} \right)_{coll} = -\frac{f(t) - f_0}{\tau}$$

Boundary conditions: \vec{E} -field in x -direction, homogenous field strength.

Ansatz: $f = f_0 + A$, $A = A(E)$...distortion term, independent of \vec{v}

$$\vec{v} \vec{\nabla}_r (f_0 + A) - \frac{eE}{m} \frac{\partial (f_0 + A)}{\partial v_x} = -\frac{1}{\tau} (f_0 + A - f_0), \text{ da } (\vec{\nabla}_r f_0 = 0)$$

$$\frac{eE}{m} \frac{\partial f_0}{\partial v_x} = \frac{1}{\tau} A$$

$$A = \frac{eE}{m} \tau \frac{\partial f_0}{\partial v_x}$$

The current density is again calculated by:

$$\vec{j}_e = -ne\vec{v} = -e \int \vec{v} \frac{dn}{V} = |dn = 2 \cdot f(\vec{v}) d\Phi| = -2e \left(\frac{m}{h} \right)^3 \frac{1}{V} \int_{\vec{R}, \vec{v}} \vec{v} f(\vec{v}) d^3x d^3v$$

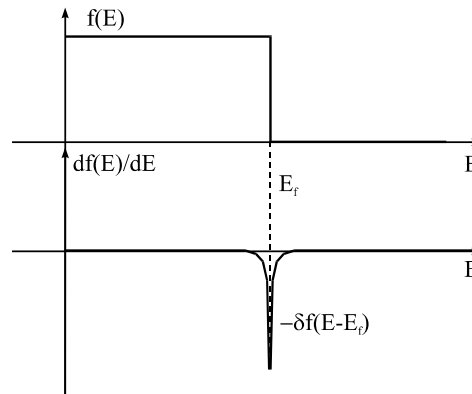
Calculation of one component of \vec{j} , j_x :

$$f = f_0 + A = f_0 + \frac{eE}{m} \tau \frac{\partial f_0}{\partial v_x}$$

$$j_x = -2e \left(\frac{m}{h} \right)^3 \frac{1}{V} \int_{\vec{R}} d^3x \int_v \underbrace{f_0(\vec{v}) v_x}_{=0} d^3v - \frac{2e^2 E}{m} \left(\frac{m}{h} \right)^3 \tau \frac{1}{V} \int_{\vec{R}} d^3x \int_v v_x \frac{\partial f_0}{\partial v_x} d^3v =$$

$$= \left| \frac{1}{V} \cdot \int_{\vec{R}} d^3x = 1 \right| = - \underbrace{2e^2 E \frac{m^2}{h^3} \tau}_{C} \int_{\vec{v}} v_x \frac{\partial f_0}{\partial v_x} d^3v$$

In the above equation only the derivation $\frac{\partial f_0}{\partial v_x}$ is unknown. It can be calculated by the known Fermi distribution and yields a Delta function (see sketch):



$$j_x = C \int_{\vec{v}} v_x \frac{\partial f_0}{\partial v_x} d^3 v = \left| d^3 v = 4\pi v^2 dv \right| = C \cdot \int_{\vec{v}} v_x \frac{\partial f_0}{\partial v_x} 4\pi v^2 dv = \left| \frac{\partial f_0}{\partial v_x} = \frac{\partial f_0}{\partial E} \frac{\partial E}{\partial v_x} = \frac{\partial f_0}{\partial E} \cdot m v_x \right| =$$

$$= C \cdot 4\pi m \int_{\vec{v}} v_x^2 \underbrace{\frac{\partial f_0}{\partial E}}_{-\delta(E-E_f)} v^2 dv$$

$$j_x = -2e^2 E \tau \frac{m^2}{h^3} \cdot 4\pi m \int_{\vec{v}} v_x^2 \cdot [-\delta(E-E_f)] v^2 dv = 8\pi e^2 E \tau \left(\frac{m}{h}\right)^3 \cdot \underbrace{\int_{\vec{v}} v_x^2 \cdot [\delta(E-E_f)] v^2 dv}_*$$

* : Solution of the integral: solve analogous equations in y and z and the determines $j_x + j_y + j_z$:

$$* = \int_{\vec{v}} [v_x^2 + v_y^2 + v_z^2] \delta(E-E_f) v^2 dv = \int_{\vec{v}} v^4 \delta(E-E_f) dv = \left| dv = \frac{dE}{mv} \right| = \int_E m^{-1} v^3 \delta(E-E_f) dE =$$

$$= \int_E m^{-1} \left(\frac{2E}{m}\right)^{3/2} \delta(E-E_f) dE = m^{-1} \left(\frac{2E_f}{m}\right)^{3/2} = m^{-1} v_f^3$$

$$j_x = \frac{1}{3} (j_x + j_y + j_z) = 8\pi e^2 E \tau \frac{m^2}{h^3} \cdot v_f^3$$

Arbitrary co ordinate system:

$$j = \frac{1}{3} j_x = \frac{8\pi e^2 E \tau m^2 v_f^3}{3h^3} E = \sigma E$$

$$\sigma = \frac{8\pi e^2 E \tau m^2 v_f^3}{3h^3} = \frac{ne^2}{m} \tau, \text{ weil}$$

$$n = \frac{1}{V} \int dn = \frac{1}{V} \int_{\vec{R}, \vec{v}} 2 f_0 \left(\frac{m}{h}\right)^3 d^3 x d^3 v = \frac{8\pi}{3} \left(\frac{v_f m}{h}\right)^3$$

c) Conductivity of thin films: Fuchs-Sondheimer-equation

Ansatz: $f = f_0 + A$, $A=A(E, z)$...distortion term, independent of \vec{v} , but now dependent on the position within the film

Possible boundary conditions:

* Specular reflection at the film interfaces: no difference to the bulk

* Diffuse reflection at the film interfaces:

Ansatz for $f(v, E, z)$: $f = f_0 + A(E, z)$

Boundary condition for diffuse reflection: $f(z=0)=f_0$

$$f(z=0) = f_0 = \underbrace{\frac{eE\tau}{m} \frac{\partial f_0}{\partial v_x}}_{A(z=0)} (1+K) + f_0$$

$$\Rightarrow K = -1$$

$$j = \underbrace{-2e \left(\frac{m}{h}\right)^3 \tau \int \vec{v} \left(f_0 + \frac{eE}{m} \frac{\partial f_0}{\partial v_x} \right) d^3v}_{j_0} + \underbrace{2e \left(\frac{m}{h}\right)^3 \tau \int \vec{v} \frac{eE}{m} \frac{\partial f_0}{\partial v_x} \cdot e^{-\frac{z}{v_z}} d^3v}_{\substack{\text{zulösen für} \\ z=0 \rightarrow z=D \\ I}}$$

For solving I the average from $z = 0$ to $z=D$ has to be calculated, then \Rightarrow script. 4.57

Appendix

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